

Integrated course „Energy Economics“ - Financial management -

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Outline

- Fundamentals of finance
- Time value of money
- Capital structure and cost of capital
- Capital budgeting: NPV method
- NPV vs IRR
- Levelised cost of electricity (LCOE)

Introduction to corporate finance

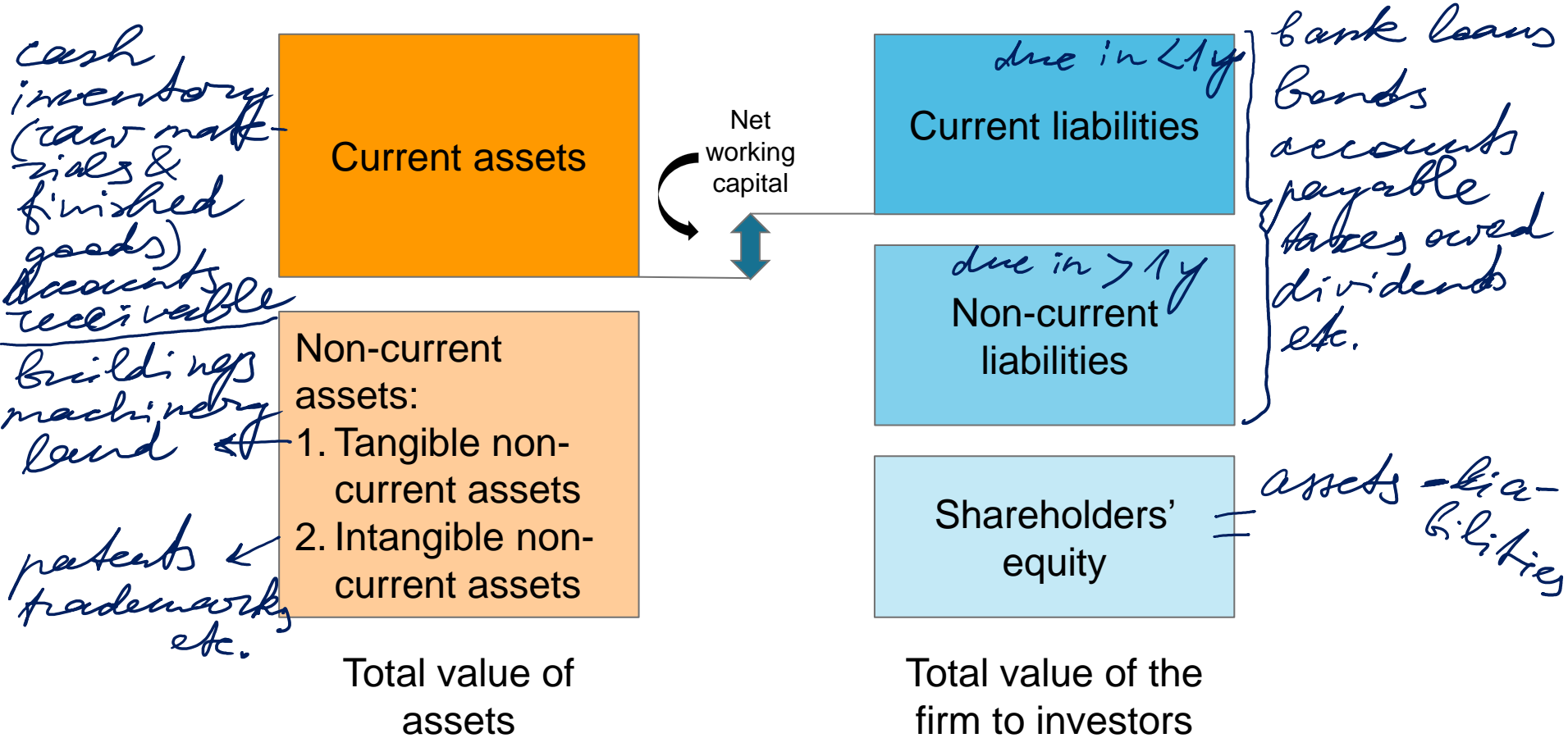
Understanding how companies invest in new projects

Starting a firm takes investment into **assets**:
inventory (raw materials), machinery, land, and labour.

The amount of cash invested into the assets has to be matched by
the amount of cash raised by **financing**.

By producing and selling products, the firm generates cash – the
basis of **value creation** for the firm's owner.

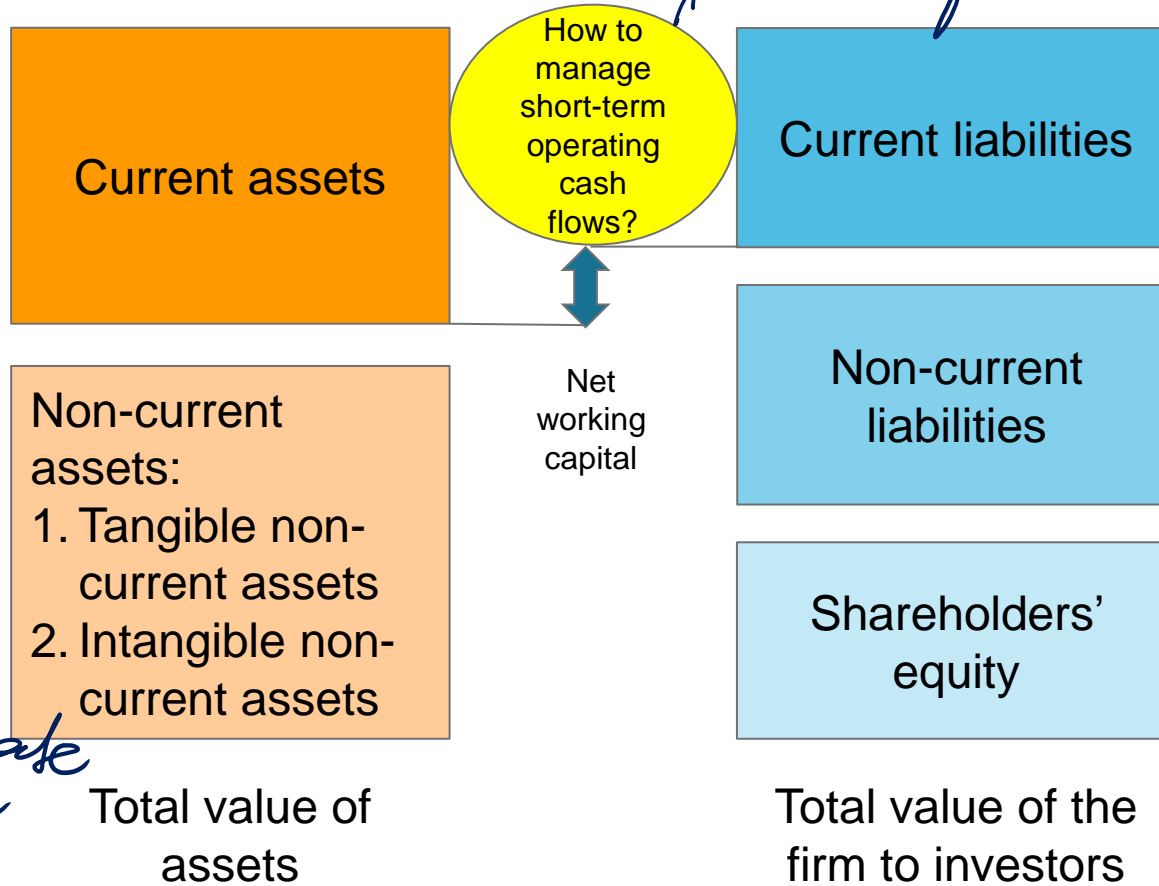
Balance sheet model of the firm



Source: Hillier, Ross, Westerfield, Jaffe, Jordan, 2016

Balance sheet model of the firm

match amounts and timing of cash inflows & outflows
→ short-term liquidity



Which long-lived assets to invest in?

buy assets that generate more cash than they cost

How to raise cash for capital expenditures?

sell bonds and shares that raise more cash than they cost

Methods of project valuation

Static methods

(single-period)

- Cost comparison statement
 - + operating costs p.a.
 - + average capital costs p.a.
 - + depreciation p.a.
 - annual costs
- Profit comparison
 - revenues ./ . annual costs
- Return on investment
 - $EBIT$ = earnings before interest and tax + interest on debt
 - $ROI = EBIT / \text{avg. capital employed p.a.}$
- Pay-back period
 - $Break\ even = \text{investment} / \text{avg. cash flow p.a.}$

Dynamic methods

(time value of money)

- Net present value
 - $PV = \text{sum of discounted cash flows}$
 - $NPV = PV - \text{Investition} > 0?$
- Equivalent annual annuity
 - transformation of cash flow series into annuity
- Internal rate of return
 - $IRR = \text{discount rate at which}$
 - $[NPV=0]$

Example: Simple payback period method

Energy saving project:

New equipment costs €3.600.

Projected annual energy cost savings: €1.200.

Payback period: $\frac{3600\text{€}}{1200\text{€/a}} = 3 \text{ years}$

Change in annual maintenance costs due to the new equipment has to be considered.

Time value of money

Value of an investment depends on the timing of cash flows.

Cash flow is an amount of money paid or received (revenue or expenditure).

Cash flows are characterised by the amount (+/-) and due date.

Time value of money: value of a cash flow at the time it becomes due.

Present value: value of a cash flow at present.

For a cash flow due and payable today:

present value = time value

For a cash flow due and payable at a future time:

present value = time value – interest

Time value of money (continued)

Two proposals for new products to choose between:
Initial cost: €10.000 in each case.

Year	New product A (€)	New product B (€)
1	0	4.000
2	0	4.000
3	0	4.000
4	20.000	4.000
Total	20.000	16.000

The investment opportunities cannot be compared immediately.

Source: Hillier, Ross, Westerfield, Jaffe, Jordan, 2016

Cashflows: Discounting and compounding

To be able to compare cashflows, they have to be discounted or compounded to the same reference period.

Choice between spending a sum of money or lending it.

Interest rate is the price for obtaining funds for a specified time.
It reflects the opportunity cost in view of other investment options and risk of credit default.

Cash flows: Compounding

- **Compounding:** Present value → future value

$$C_T = C_0 \cdot (1 + i)^T$$

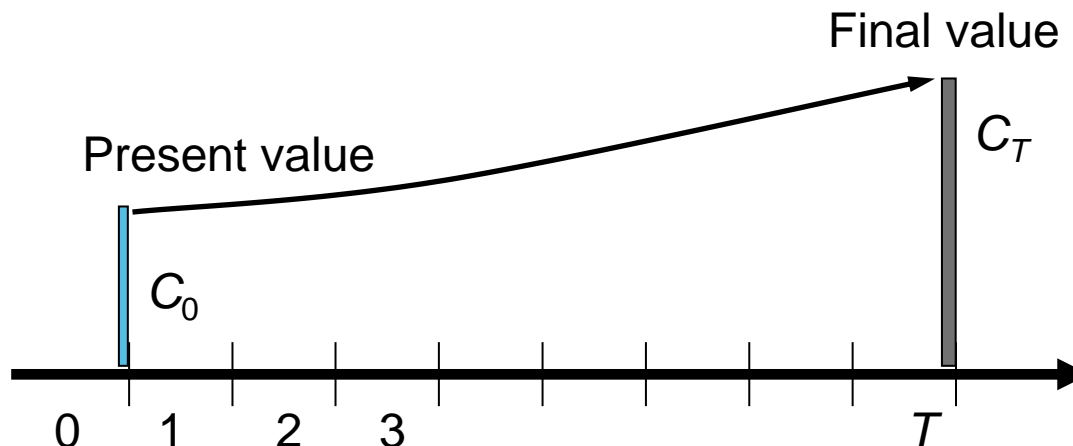
C_0 = the cash flow at date 0 (today) = present value

i = interest rate per period

T = number of periods (time horizon)

C_T = value of the cash flow at time T = future value

Compound interest:
 $C_0 \cdot (1+i)$ → lended again after 1 period
 $(C_0(1+i)) \cdot (1+i)$ → lended again etc. after 1 period



Cash flows: Discounting

- **Discounting:** Future value \rightarrow present value

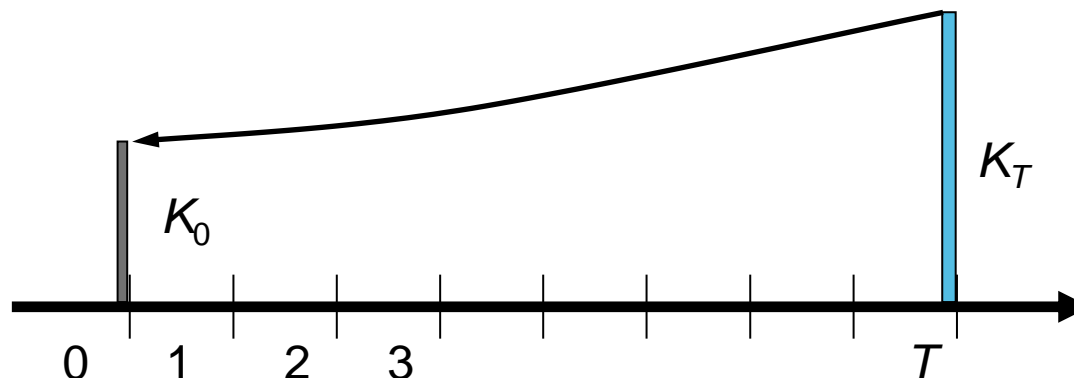
$$C_0 = C_T \cdot \frac{1}{(1 + i)^T}$$

C_0 = value of the cash flow at date 0 (today) = present value

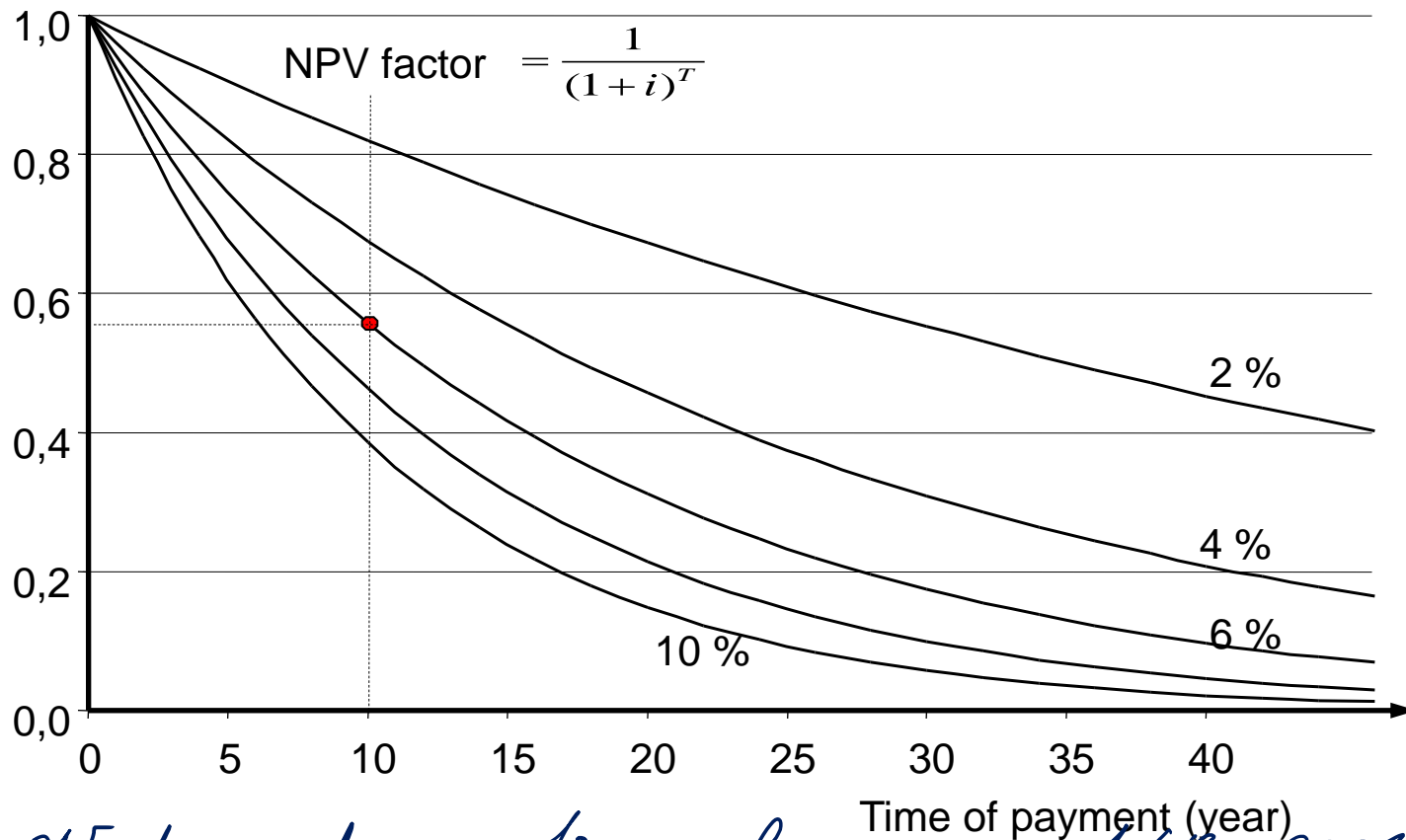
i = interest rate per period

T = number of periods (time horizon)

C_T = the cash flow at time T = future value



Present value of a future cash flow

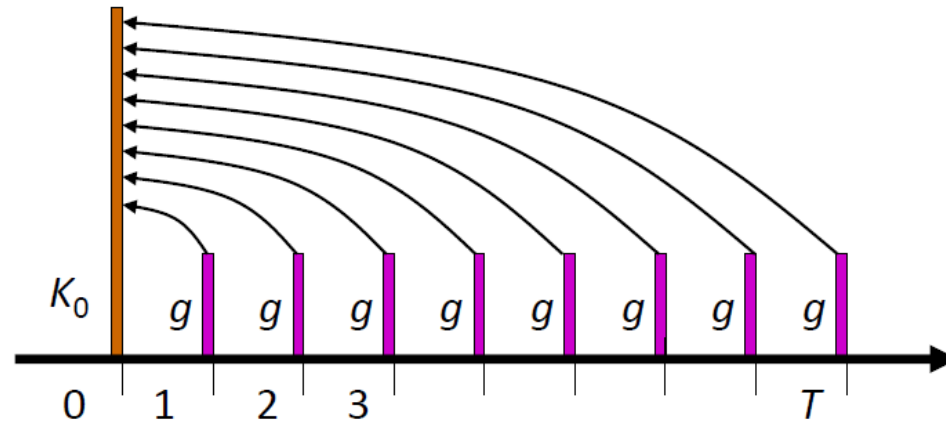


PV depends on time of payment (the sooner, the higher PV) and on the interest rate (the lower the interest rate, the higher PV).

Annuity: NPV with constant cash flows

Annuity is a level stream of regular payments during a fixed number of periods.

K_0 = Present value
 g = Periodical payment
 i = Interest rate
 $q = (1+i)$ Interest factor
 T = Number of periods



Value at the end
of period 0

$$K_0 = g \cdot \left(1 + \frac{1}{q} + \frac{1}{q^2} + \dots + \frac{1}{q^T} \right) = g \cdot \frac{q^T - 1}{q - 1} \cdot \frac{1}{q^T} = g \cdot \frac{1 - q^{-T}}{q - 1}$$

$$K_0 = g \cdot \frac{q^T - 1}{q - 1} \cdot \frac{1}{q^T} = g \cdot \frac{1 - q^{-T}}{q - 1}$$

$$K_0 = g \cdot \text{Annuity factor}_{i,T} \quad \text{with} \quad \text{Annuity factor}_{i,T} = \frac{1}{i} - \frac{1}{i(1+i)^T}$$

Annuity factor

Years	Interest rate [%]									
	3.0	3.5	4.0	4.5	5.0	6.0	7.0	8.0	9.0	10.0
1	0.971	0.966	0.962	0.957	0.952	0.943	0.935	0.926	0.917	0.909
2	1.913	1.900	1.886	1.873	1.859	1.833	1.808	1.783	1.759	1.736
3	2.829	2.802	2.775	2.749	2.723	2.673	2.624	2.577	2.531	2.487
4	3.717	3.673	3.630	3.588	3.546	3.465	3.387	3.312	3.240	3.170
5	4.580	4.515	4.452	4.390	4.329	4.212	4.100	3.993	3.890	3.791
6	5.417	5.329	5.242	5.158	5.076	4.917	4.767	4.623	4.486	4.355
7	6.230	6.115	6.002	5.893	5.786	5.582	5.389	5.206	5.033	4.868
8	7.020	6.874	6.733	6.596	6.463	6.210	5.971	5.747	5.535	5.335
9	7.786	7.608	7.435	7.269	7.108	6.802	6.515	6.247	5.995	5.759
10	8.530	8.317	8.111	7.913	7.722	7.360	7.024	6.710	6.418	6.145
11	9.253	9.002	8.760	8.529	8.306	7.887	7.499	7.139	6.805	6.495
12	9.954	9.663	9.385	9.119	8.863	8.384	7.943	7.536	7.161	6.814
13	10.635	10.303	9.986	9.683	9.394	8.853	8.358	7.904	7.487	7.103
14	11.296	10.921	10.563	10.223	9.899	9.295	8.745	8.244	7.786	7.367
15	11.938	11.517	11.118	10.740	10.380	9.712	9.108	8.559	8.061	7.606
20	14.877	14.212	13.590	13.008	12.462	11.470	10.594	9.818	9.129	8.514
25	17.413	16.482	15.622	14.828	14.094	12.783	11.654	10.675	9.823	9.077
30	19.600	18.392	17.292	16.289	15.372	13.765	12.409	11.258	10.274	9.427
35	21.487	20.001	18.665	17.461	16.374	14.498	12.948	11.655	10.567	9.644
40	23.115	21.355	19.793	18.402	17.159	15.046	13.332	11.925	10.757	9.779
45	24.519	22.495	20.720	19.156	17.774	15.456	13.606	12.108	10.881	9.863
50	25.730	23.456	21.482	19.762	18.256	15.762	13.801	12.233	10.962	9.915

Capital recovery factor

$$CRF = \frac{1}{AF}$$

Years	Interest rate [%]									
	3.0	3.5	4.0	4.5	5.0	6.0	7.0	8.0	9.0	10.0
1	1.030	1.035	1.040	1.045	1.050	1.060	1.070	1.080	1.090	1.100
2	0.523	0.526	0.530	0.534	0.538	0.545	0.553	0.561	0.568	0.576
3	0.354	0.357	0.360	0.364	0.367	0.374	0.381	0.388	0.395	0.402
4	0.269	0.272	0.275	0.279	0.282	0.289	0.295	0.302	0.309	0.315
5	0.218	0.221	0.225	0.228	0.231	0.237	0.244	0.250	0.257	0.264
6	0.185	0.188	0.191	0.194	0.197	0.203	0.210	0.216	0.223	0.230
7	0.161	0.164	0.167	0.170	0.173	0.179	0.186	0.192	0.199	0.205
8	0.142	0.145	0.149	0.152	0.155	0.161	0.167	0.174	0.181	0.187
9	0.128	0.131	0.134	0.138	0.141	0.147	0.153	0.160	0.167	0.174
10	0.117	0.120	0.123	0.126	0.130	0.136	0.142	0.149	0.156	0.163
11	0.108	0.111	0.114	0.117	0.120	0.127	0.133	0.140	0.147	0.154
12	0.100	0.103	0.107	0.110	0.113	0.119	0.126	0.133	0.140	0.147
13	0.094	0.097	0.100	0.103	0.106	0.113	0.120	0.127	0.134	0.141
14	0.089	0.092	0.095	0.098	0.101	0.108	0.114	0.121	0.128	0.136
15	0.084	0.087	0.090	0.093	0.096	0.103	0.110	0.117	0.124	0.131
20	0.067	0.070	0.074	0.077	0.080	0.087	0.094	0.102	0.110	0.117
25	0.057	0.061	0.064	0.067	0.071	0.078	0.086	0.094	0.102	0.110
30	0.051	0.054	0.058	0.061	0.065	0.073	0.081	0.089	0.097	0.106
35	0.047	0.050	0.054	0.057	0.061	0.069	0.077	0.086	0.095	0.104
40	0.043	0.047	0.051	0.054	0.058	0.066	0.075	0.084	0.093	0.102
45	0.041	0.044	0.048	0.052	0.056	0.065	0.073	0.083	0.092	0.101
50	0.039	0.043	0.047	0.051	0.055	0.063	0.072	0.082	0.091	0.101

Outlook: $NPV = -I_0 + DCF$ - see below slides

$$NPV_A = -10\,000\text{€} + 17\,094\text{€} = \underline{7\,094\text{€}}$$

$$NPV_B = -10\,000\text{€} + 14\,520\text{€} = \underline{4\,520\text{€}}$$

Solution to previous example

Two proposals for new products to choose between:

Initial cost: €10.000 in each case. Find PV of revenues for A and B.

Year	New product A (€)	New product B (€)
1	0	4.000
2	0	4.000
3	0	4.000
4	20.000	4.000
Total	20.000	16.000

annuity
 $PV_{annuity} = g \cdot AF_{i,T}$
 $AF_{4\%,4y} = 3,630$
 (see table)
 $PV_B = 4000\text{€} \cdot 3,630 = 14.520\text{€}$

The interest rate is 4%. $PV(CF_T) = \frac{CF_T}{(1+i)^T}$

$$PV_B = \frac{20\,000\text{€}}{(1+0,04)^4} = \frac{20\,000}{1,17} = \underline{17.094\text{€}} \rightarrow PV_A > PV_B$$

Source: Hillier, Ross, Westerfield, Jaffe, Jordan, 2016

Discount rate

The discount rate represents cost of capital and project risk.

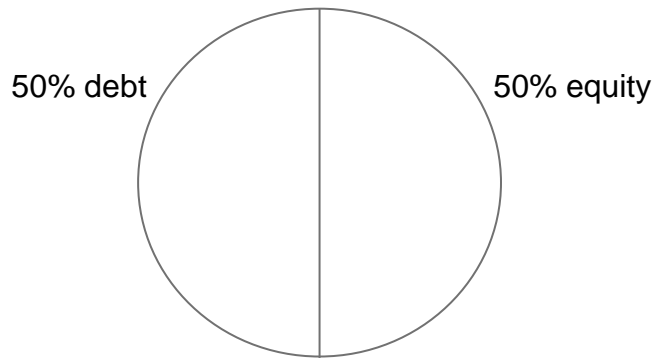
↙ Risk-free interest rate + risk premium

*opportunity to buy
government bonds*

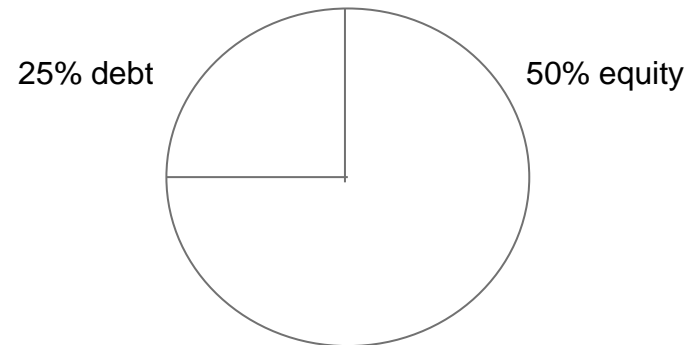
How to raise cash for capital expenditures?

- Equity (own capital) – raised from shareholders
 - rewarded by dividends + the difference in the market price of shares (if positive)
 - right to share in assets remaining after liabilities in case of liquidation
 - participate in managing the firm
- Debt (borrowed capital) – borrowed from creditors /debtholders
 - rewarded through interest
 - preferred over shareholders (incl. in case of bankruptcy)

Capital structure: Weighted average cost of capital (WACC)



Capital structure 1



Capital structure 2

$$WACC = \frac{E}{D + E} (r_e) + \frac{D}{D + E} (r_d)(1 - t)$$

Where:

E = market value of equity

D = market value of debt

r_e = cost of equity

r_d = cost of debt

t = corporate tax rate

interest tax shield

→

↓

The amount of interest paid on debt is deducted from the taxable income. This reduces the income tax paid by the company.